

BUCKLING ASSESSMENT OF IMPERFECT CYLINDRICAL SHELLS UNDER AXIAL LOADS USING A GEP TECHNIQUE

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Abstract: Determination of buckling behavior of shell structures has long been identified as a challenging task. This is largely because the buckling behavior is masked by local large deformations, which occur once the critical load is reached. This research proposes a novel technique to accurately predict the buckling load of imperfect cylindrical shells using gene expression programming (GEP), which is an evolutionary artificial intelligence method. An existing experimental data bank was employed for training and testing the program, and the obtained buckling load of shell structures were accordingly verified. From the results, it is concluded that GEP is a promising and reliable method to determine the buckling load of shell structures subjected to axial compression.

Keywords: Gene expression programming technique; shell structures; buckling load; axial compression

PROCJENA IZVIJANJA NESAVRŠENE CILINDRIČNE LJUSKE PRI OSNOM OPTEREĆENJU PRIMJENOM GEP TEHNIKE

Sažetak: Definiranje ponašanja pri izvijanju odavno je identificirano kao izazovan zadatak pri izučavanju plošnih konstrukcija. Razlog tomu je činjenica da lokalne velike deformacije nastaju nakon dosezanja kritičnog opterećenja pa je opće ponašanje pri izvijanju prikriveno tim deformacijama. Ovo istraživanje predlaže novi pristup za precizno određivanje sile pri izvijanju kod nesavršenih cilindričnih ljuski, primjenom programiranja genetičkim izrazom (GEP), evolucijske metode umjetne inteligencije. Za učenje i testiranje programa primijenjena je postojeća eksperimentalna baza podataka te je predložen izraz za silu pri izvijanju plošnih konstrukcija, koji je sukladno tome i verificiran. Zaključeno je da je GEP obećavajuća i pouzdana metoda za određivanje sile izvijanja kod osno naprezanih plošnih konstrukcija.

Ključne riječi: tehnika programiranja genetičkim izrazom; plošne konstrukcije; sila pri izvijanju; osno tlačno naprezanje

Buckling assessment of imperfect cylindrical shells under axial loads using a GEP technique



1 INTRODUCTION

Stiffened and unstiffened cylindrical shells are widely used in many applications such as in offshore structures, where their application is crucial. For these cylindrical shells subjected compressive loads, the buckling limit state needs to be considered because it has been reported that buckling is the primary limit state for cylindrical shells compared to plates and columns. Furthermore, the stability of shell structures is also governed by the buckling behavior [1, 2]. Hence, many researchers have studied this behavior to determine the most accurate capacity of cylindrical shells under compressive loads. On the other hand, the buckling analysis of such structures is considered a serious challenge, since the buckling load cannot be easily determined from the data analysis of experimental results [3, 4]. Generally, shell structures exhibit significant initial geometric imperfections; hence, the determination of their buckling load has been reported to be approximate and imprecise [5]. Figure 1 illustrates the geometric features of a cylindrical shell structure with general geometric parameters.



Figure 1 Geometric features of cylindrical shell structures

The stability of slender columns under compressive loads is assessed by the classical buckling theory of elastic structures proposed in Euler's investigations. The governing linear equations are solved by eigenvalue analysis to obtain the buckling loads and the corresponding failure modes as eigenvalues and eigenvectors, respectively [6]. However, experimental investigations and developments in metal constructions demonstrated that:

- a) The classical buckling theory assessment generally overestimates the experimental buckling loads.
- b) Wide ranges of buckling loads are obtained for similar specimens.
- c) Catastrophic limit state failure occurred for significant number of specimens.

These findings prove the insufficiency of the classical buckling theory in specific applications, which necessitate further studies related to thin-shell structures.

There are many studies investigating the buckling behavior of shell structures to estimate the critical buckling load. Waszczyszyn and Bartczak investigated the critical buckling load of cylindrical shells with geometric imperfections using neural prediction and concluded that the application of imperfection parameters is an efficient method to analyze the experimental results of the buckling investigations [7]. They continued the research of Tadeusiewicz et al., who employed back-propagation neural networks (BPNNs) to determine the buckling load of cylindrical shells under axial compression [8]. Most recently, Ghanbari Ghazijahani and Zirakian investigated the critical buckling load of thin shells by implementing extrapolation techniques [5]. The efficiency of Southwell, Massey, Modified, and Meck plotting methods in investigating the buckling behavior of shell structures were confirmed in their study.

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Soft computing techniques have been employed to solve many structural engineering problems [9-12]. A novel soft computing technique, genetic programming (GP), was developed for engineering modeling [13-15]. In this method, program space is considered instead of data space, which facilitates the generation of prediction equations without prior assumptions. A number of studies implemented GP methodologies to identify complex relationships corresponding to the experimental data [16, 17]. The gene expression programming (GEP), an extension of GP, has also been adopted in a number of studies, where programs of various sizes and shapes were developed in the form of linear chromosomes of fixed length. The GEP chromosomes consist of multiple genes, and each gene has a smaller subprogram. The GEP has been reported to be an efficient and applicable method compared to the previous traditional soft computing techniques (e.g., GP), which are used in limited number of studies on structural applications.

Unlike the regression techniques, which were being used previously, the GEP implements a trial-and-error method in a regular process of system identification; therefore, a structure can be modeled to fit appropriately with the training data [18]. In this research, the buckling load prediction was explored in detail using the GEP. A formula was derived by training the software using input data procured from the Delft University of Technology experimental data bank [19].

2 GENE EXPRESSION PROGRAMMING

2.1 Brief outlook

GEP, initially proposed by Ferreira, implements the principles of GA and genetic programming (GP) [20]. The GEP evaluation strategy of any scientific data is similar to the biological evaluation. GEP has five main components: (i) terminal set, (ii) functional set, (iii) fitness function, (iv) algorithm control parameters, and (v) termination criterion [21]. The search space is identified by the first three components, while the quality and speed of the search is governed by the last two components.

The GEP-based models and the corresponding equations, which are based on existing experimental data, differ from the conventional models, which were developed based on the general engineering principles such as the basic theories of elasticity and/or plasticity. Subsequently, modeling uncertainties resulting from simplifications and assumptions are significantly reduced [21].

As illustrated in Figure 2, in GEP algorithm, a random generation is developed from the initial generation. The chromosomes are accordingly converted into "an expression tree," and the fitness of each chromosome is computed. Further, the chromosomes are chosen based on their fitness, to be reproduced with proper modifications. The chromosomes of the new generation are subjected to similar developmental process, i.e., "expression of the genomes," "confrontation of the selection environment," and "reproduction with modification" [22]. This process is repeated until a satisfactory solution is obtained.





Figure 2 GEP flowchart [20]

2.2 GEP features in this study

In this study, a soft computation technique, the GEP, was performed to predict the axial buckling load of shell structures. The function set consisted of eight basic arithmetic operators (+, -, ×, \div , $\sqrt{}$, ln, exp, power) and constants. The terminal set included four fundamental parameters of P_{cr} , as given in Eq. (1) [23].

$$P_{cr} = f(E, R, t, L) \tag{1}$$

where P_{cr} corresponds to the critical buckling load of the shell specimen; *E*, the Young's modulus; R, the radius; *t*, the thickness; and *L*, the length. It has been previously reported that the geometric parameters— including mostly the above parameters—significantly affect the buckling strength of shells [1, 24, 25]. Further, in this GEP model, the number of genes was considered as 2, mutation rate as 0.044, inversion rate as 0.1, one-point and two-point recombination rates as 0.3, and gene recombination and transportation rates as 0.1. During the training and testing of the GEP model, *R*, *t*, *L* and *E* were considered as input data (see Figure 1); hence, P_{cr} was obtained as an independent

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output in this study. Furthermore, this study was based on the recorded imperfections and shell specimen tests from the experimental data bank [19]. Table 1 summarizes the details of the specimens employed to train the soft computing model of GEP.

3 ANALYSES AND DISCUSSIONS

3.1 GEP output for critical buckling load

Among 35 experimental data from the data bank, 26 were randomly selected as the training set and the rest were used to test the proposed model's generalization capacity. The simplified analytic form of the proposed GEP model, expressed as Eq. (2), was eventually achieved; where $C_0 = 4.65$ and $C_1 = 9.84$ are constants.

$$P_{cr} = E^{C_0^2 \frac{t}{R}} L^{C_1 \frac{t}{R}} R^2$$
(2)

3.2 Performance measures

The accuracy and performance of the proposed formula were evaluated considering several statistical verification criteria such as the square correlation coefficient (R^2), the root mean square error (*RMSE*) and the mean absolute error (*MAE*). This evaluation was conducted to simultaneously obtain high R^2 and low *RMSE* and *MAE* values, which signify the most precise approximation. These criteria can be calculated based on equations (3)–(5):

$$R^{2} = 1 - \frac{\sum_{i=1}^{n} (p_{i} - o_{i})^{2}}{\sum_{i=1}^{n} (o_{i} - \overline{o_{i}})^{2}}$$

$$RMSE = \sqrt{\frac{\sum_{i=1}^{n} (p_{i} - o_{i})^{2}}{n}}$$
(3)
(4)

$$MAE = \frac{\sum_{i=1}^{n} |p_i - o_i|}{n}$$
(5)

where p_i indicates the predicted values of the buckling load, n is the number of data and o_i and $\overline{o_i}$ denote the observed and average observed experimental output values of the buckling load, respectively. It was observed that the performance of the metaheuristic algorithms could not be assessed from the results of a single run due to the random nature of the computations. Hence, training and testing were intermittently conducted to reduce any possible errors.

Comparison of the predicted values with the measured values is presented in Figure 3. The efficiency and precision in the learning of the proposed model was demonstrated by the training set results. The comparison of the values obtained from the GEP method with the corresponding experimental results demonstrates the high generalization capacity of the proposed models and the low error values obtained by implementing the proposed equations. Hence, it can be concluded that this method can derive a nonlinear relationship between the input and the output parameters,

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with high correlation and comparatively low errors. Table 2 presents the results of statistical analysis of the results obtained from training and testing sets in detail.



Model (N)

(a)



(b)

Figure 3 Correlation of the measured and predicted values in: (a) training and (b) testing stages

The values of R², RMSE, and MAE calculated with the results of the training and testing sets indicate that GEP can be reliably utilized to predict the buckling load of shell structures under axial compressive load during both training and testing stages. The curve fitting, target sorted fitting, and standard distributions of both training and testing stages are depicted in Figures 4–6, respectively. The results demonstrate that the proposed model can follow the targeted curve values with satisfactory accuracy.

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Figure 4 The curve fitting for (a) training and (b) testing stages





(b) Figure 5 Target sorted fitting for (a) training and (b) testing stages





(b) Figure 6 The standard distributions for (a) training and (b) testing stages

Table 2. Statistical	values of P _{cr} from the GEP model	
Statistical parameters	Training set	Testing set
R^2	0.9997	0.9417
RMSE	8130.49	6305.57
MAE	6442.09	5704

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4 CONCLUSIONS

The difficulties in creating buckling load prediction models using classical GP and GEP techniques were identified. It has been reported that the performance of these models cannot be enhanced by using a number of expressions and complicated functions or by changing the runtime and the depth of genes. However, such measures might result in over-trained models after some generations. This study proposes a hybrid model of GEP-GA, which implements the principles of GA into GEP technique to improve the performance by creating gene weights for obtaining GEP expressions.

The efficiency of GEP technique in estimating the buckling load of imperfect cylindrical shells under axial compressive load was investigated. The experimental results obtained from previous literature and the proposed empirical model were utilized to study the buckling behavior of shell structures under axial loads. The study was conducted on two sets of data (training and testing data), which were based on the recorded geometric imperfections and the buckling load from experimental results.

The results obtained from the model showed an excellent agreement with the experimental data, and the statistical parameters R2, MAE, and RMSE indicated a good precision. Hence, it is concluded that GEP can be reliably utilized to predict the buckling load of shell structures subjected to axial compressive loads in both training and testing stages.

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Appendix

Table 1 Experimental database obtained from the data bank [19]									
<i>R</i> (mm)	<i>t</i> (mm)	<i>L</i> (mm)	<i>E</i> (MPa)	$P_{cr}(N)$					
101.6	0.0986	196.85	172400	2676.5					
101.6	0.0975	196.85	172400	3048.8					
101.6	0.0978	196.85	172400	3905.5					
101.6	0.205	196.85	106500	11326					
101.6	0.1852	144.78	106500	7178.5					
101.6	0.2634	140.97	106500	16661.2					
117.86	0.4564	148.59	180600	56050					
118.36	0.4526	148.59	180600	48500					
117.91	0.46	148.59	180600	46800					
118.49	0.4554	148.59	180600	51350					
118.49	0.4567	148.59	180600	49900					
117.86	0.4544	148.59	180600	41700					
101.6	0.236	133.35	68950	12986.5					
101.6	0.2413	133.35	68950	15060.3					
101.6	0.2553	133.35	68950	17967.2					
101.6	0.2649	133.35	68950	18575.7					
101.6	0.2131	133.35	68950	12224.1					
101.6	0.2149	133.35	68950	12277.5					
101.6	0.2098	146.3	68950	9742.9					
101.6	0.2116	139.7	68950	14286.3					
101.6	0.2238	139.7	68950	15107.4					
101.6	0.2065	137.16	68950	16997.9					
	Table 1 Expe R (mm) 101.6 101.6 101.6 101.6 101.6 101.6 101.6 101.6 101.6 101.6 101.6 117.86 118.49 117.86 101.6	Table 1 Experimental database R (mm) t (mm)101.60.0986101.60.0975101.60.0978101.60.205101.60.1852101.60.2634117.860.4564118.360.4526117.910.46118.490.4554117.860.4544101.60.236101.60.2413101.60.2553101.60.2649101.60.2131101.60.2149101.60.2149101.60.2116101.60.2238101.60.2238101.60.2238101.60.2238101.60.2238101.60.2238101.60.2238	Table 1 Experimental database obtained from R (mm) t (mm) L (mm)101.60.0986196.85101.60.0975196.85101.60.205196.85101.60.205196.85101.60.2634140.97101.60.2634140.97117.860.4564148.59118.360.4526148.59117.910.46148.59118.490.4554148.59117.860.4544148.59117.860.4544148.591160.236133.35101.60.2649133.35101.60.2649133.35101.60.2131133.35101.60.2131133.35101.60.2149133.35101.60.2116139.7101.60.2238139.7101.60.2065137.16	Table 1 Experimental database obtained from the data bank [19] R (mm) t (mm) L (mm) E (MPa)101.60.0986196.85172400101.60.0978196.85172400101.60.205196.85106500101.60.205196.85106500101.60.2634140.97106500101.60.2634140.97106500101.60.2634148.59180600117.860.4564148.59180600118.360.4526148.59180600117.910.46148.59180600118.490.4554148.59180600117.860.4544148.59180600117.860.4567148.59180600101.60.236133.3568950101.60.2413133.3568950101.60.2649133.3568950101.60.2131133.3568950101.60.2149133.3568950101.60.2116139.768950101.60.2238139.768950101.60.2238137.1668950					

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23	101.6	0.2649	141.73	68950	24950.4
24	101.6	0.236	133.35	68950	12986.5
25	101.6	0.2413	133.35	68950	15060.3
26	101.6	0.2553	133.35	68950	17967.2
27	101.6	0.2649	133.35	68950	18575.7
28	101.6	0.2131	133.35	68950	12224.1
29	101.6	0.2149	133.35	68950	12277.5
30	101.6	0.2098	146.3	68950	9742.9
31	101.6	0.2116	139.7	68950	14286.3
32	101.6	0.2238	139.7	68950	15107.4
33	101.6	0.2065	137.16	68950	16997.9
34	101.6	0.2649	141.73	68950	24950.4
35	946.2	0.6426	2743.2	68950	1138325

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